Zhang, Lei
Abundance for 3-folds with non-trivial Albanese maps in positive characteristic. (English)

In recent years, many of the results of the Minimal Model Program have been extended from characteristic zero to characteristic \( p > 5 \). For example, existence of log minimal models of threefolds has been proved by C. Birkar [Ann. Sci. Éc. Norm. Supér. (4) 49, No. 1, 169–212 (2016; Zbl 1346.14040)], C. D. Hacon and C. Xu [J. Am. Math. Soc. 28, No. 3, 711–744 (2015; Zbl 1326.14032)]. There has also been significant progress on the log abundance conjecture. In the case of threefold klt pairs, it has been proved when the variety is of log general type or when the boundary divisor is big (in addition to the above references, see also [P. Cascini et al., Ann. Sci. Éc. Norm. Supér. (4) 48, No. 5, 1239–1272 (2015; Zbl 1408.14020] and [C. Xu, J. Inst. Math. Jussieu 14, No. 3, 577–588 (2015; Zbl 1346.14020)]).

In the present paper, the author builds upon his previous work [L. Zhang, J. Lond. Math. Soc., II. Ser. 99, No. 2, 332–348 (2019; Zbl 1410.14013)] and proves abundance for threefolds with non-trivial Albanese map.

Theorem 1.1. Let \( X \) be a klt, \( \mathbb{Q} \)-factorial, projective minimal threefold defined over an algebraically closed field \( k \) of characteristic \( p > 5 \). Assume that the Albanese map is non-trivial. Then \( K_X \) is semi-ample.

The author also proves some instances of log abundance.

Theorem 1.2. Let \((X, B)\) be a klt, \( \mathbb{Q} \)-factorial, projective minimal pair of dimension three defined over an algebraically closed field of characteristic \( p > 5 \). Assume that the Albanese map \( \alpha_X \) is non-trivial. Denote by \( f : X \to Y \) the fibration arising from the Stein factorization of \( \alpha_X \) and by \( X_\eta \) the generic fiber of \( f \). Assume moreover that \( B = 0 \) if

1. \( \dim(Y) = 2 \) and \( \kappa(X_\eta, (K_X + B)|_{X_\eta}) = 0 \), or
2. \( \dim(Y) = 1 \) and \( \kappa(X_\eta, (K_X + B)|_{X_\eta}) = 1 \).

Then \( K_X + B \) is semi-ample.

Reviewer: Justin Lacini (Lawrence)

MSC:
14E30 Minimal model program (Mori theory, extremal rays)
14E05 Rational and birational maps

Keywords:
abundance; positive characteristic; Albanese map

Full Text: DOI

References:


Mukai, S.: Duality betweenD(X) andD(X)ˆ with its application to Picard sheaves. Nagoya Math. J.81, 153-175 (1981)Zbl 0491.14006 MR 0637060 · Zbl 0491.14006


Edited by FIZ Karlsruhe, the European Mathematical Society and the Heidelberg Academy of Sciences and Humanities © 2022 FIZ Karlsruhe GmbH Page 2
algebraica, Mexico, 24-53 (1958); Oeuvres, Vol. 1, 501-530 (1958) Zbl 0098.13103 MR 0098097


[47] Zhang, L.

This reference list is based on information provided by the publisher or from digital mathematics libraries. Its items are heuristically matched to zbMATH identifiers and may contain data conversion errors. It attempts to reflect the references listed in the original paper as accurately as possible without claiming the completeness or perfect precision of the matching.